

EFFECT OF ANTIMONY SUBSTITUTION FOR NIOBIUM ON THE CRYSTAL STRUCTURE, PIEZOELECTRIC AND DIELECTRIC PROPERTIES OF $(\text{K}_{0.5}\text{Na}_{0.5})\text{NbO}_3$ CERAMICS

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Abstract

The effect of antimony substitution for niobium on potassium sodium niobate (KNN) ceramic was investigated with respect to the densification behaviour at different sintering temperatures, microstructure and electrical properties. Sb^{5+} was slightly added while simultaneously lowering the amount of Nb^{5+} and in this study of the $(\text{K}_{0.5}\text{Na}_{0.5})(\text{Nb}_{1-x}\text{Sb}_x)\text{O}_3$ system, x content was varied from 0 to 14 mol.%. Our results show that Sb^{5+} slightly increased the optimum sintering temperature for KNN but above 8 mol %, its resistivity and piezoelectric properties decreased. As the amount of Sb^{5+} substituted is increased, the structure of the ceramic transformed from orthorhombic to pseudo-cubic which led to slight shrinkage in the unit cell volume. Microstructural examination revealed that above 10 mol %, a second phase ($\text{K}_2\text{NaSb}_3\text{O}_9$) was formed which segregated mainly to the grain boundary while the quantitative EDX analysis showed that there was A-site vacancy due to loss of the alkali elements. The two phase transitions points, Curie temperature (T_C) and the tetragonal to orthorhombic (T_{T-O}) shifted to lower temperature with increasing Sb^{5+} content and above 10 mol %, the T_{T-O} shifted to below room temperature. The dielectric loss slightly increases with increasing Sb^{5+} content up to 200°C. There was an improvement in the piezoelectric properties with ≤ 6 mol % Sb content while optimum properties were obtained with 4 mol % ($K_P = 0.46$, $Q_m = 6.2$, $N_P = 2296$).

I. Introduction

Research into lead free single and polycrystalline potassium sodium niobate (KNN) piezoelectric ceramics started in the 1950'S. Eric Cross investigated the electric double hysteresis in KNN single crystals from which a part of the present phase diagram was obtained¹. Jaeger et al showed that with hot pressing, the relative density, piezoelectric and electromechanical properties of KNN can be greatly improved². Egerton et al compared the dielectric, piezoelectric and electromechanical properties of KNN, KNbO_3 and NaNbO_3 respectively and made the first sketch of the whole phase diagram for KNN³.

With the discovery of ferroelectric properties in lead zirconate titanate (PZT) ceramics, research interest in KNN slowed down due to the fact that the piezoelectric properties obtained in the former far exceeded that from the latter and also due to its complicated processing steps. Environmental concerns and government legislation in recent years have made it possible for research activity into lead free piezoelectric ceramics to increase once again⁴. Efforts are being made in recent times to improve the properties and sinterability of KNN through different synthesis routes while avoiding pressure assisted methods because they are very expensive. Kosec et al⁵ used activated sintering to improve the properties of KNN by using excess Nb^{5+} , alkali oxides amount and Mg as additive. Spark plasma sintering has also been used to obtain densities above 99 % of the theoretical density and good piezoelectric properties⁶. Recently, a modified chemical approach with urea to reduce the temperature (550°C) required for calcination has been reported but the properties were not measured to confirm that good

piezoelectric properties can be obtained⁷. Saito et al^{8,9} showed that by using texture and isovalent substitution of both the A and B-site elements, the piezoelectric properties in the KNN system can be greatly improved. Combined Li⁺, Ta⁵⁺ and Sb⁵⁺ substitutions have been known to give the highest piezoelectric properties in the KNN system^{10,11}. The effect of Li⁺ on the properties of KNN have also been widely reported in the literature^{12,13}. The effect of Ta⁵⁺ which is expected to enter the B-site of the structure based on valence and ionic radius has also been reported by Matsubara et al¹⁴. Li⁺ and Ta⁵⁺^{9,15} as well as Li⁺ and Sb⁵⁺ on the A and B-sites respectively of KNN have been reported^{16,17}. There is however very little report in the literature on the effect of adding only Sb⁵⁺ on the structure and properties of KNN. KNN has been doped with Sb and MnO₂ and the authors reported that MnO₂ served only as a sintering aid but it is possible that it has other effects on KNN^{18,19}. In this work, we investigated the effect of substituting Nb⁵⁺ with Sb⁵⁺ on the piezoelectric, dielectric, crystallographic and microstructural properties of K_{0.5}Na_{0.5}NbO₃. The objective was to understand through experimental studies, what happens when only Nb⁵⁺ is substituted with Sb⁵⁺ in KNN.

II. Experimental Procedure

(K_{0.5}Na_{0.5})(Nb_{1-x}Sb_x)O₃ [x= (0; 0.02; 0.14)] was synthesized through the mixed oxide route from the following powders; K₂CO₃, Na₂CO₃, (99%), Nb₂O₅ and Sb₂O₃ (99.9%) (Chempur Feinchemikalien und Forschungs GmbH, Karlsruhe, Germany). The powders were mixed and attrition milled for 2 h using ethanol as solvent and 3 mm zirconia balls as the milling media. They were then calcined at 800°C for 4 h in air; the milling step was repeated to homogenize the powder and also to reduce the average particle size.

The powders were put inside a custom made silicone mould and pressed for 2 min at 500 MPa with a cold isostatic press to obtain pellets with approximately 8.0 mm diameter and 2.7 mm thickness. Sintering was carried out at 1080°C, 1090°C and 1100°C respectively for 2 h in air.

The relative density values of the samples were calculated using the Archimedes method and after that, they were ground and polished and chemically etched for characterization. The crystal structures of the sintered samples were examined using X-ray diffraction (XRD) with CuK α radiation (λ =1.54178 Å) (D8 Discover, Bruker AXS, Karlsruhe, Germany) while the whole powder pattern decomposition was done with the Le Bail fitting method in Topas. Some samples (x=0, 0.02, 0.06, 0.1, 0.12 0.14) sintered at 1080°C were thermally etched at a heating/cooling rate of 10°C/min to 925°C for 30 min. Microstructural examination and quantitative Energy dispersive spectroscopy (EDX) (Oxford Instruments) element analysis of the samples were done using a scanning electron microscope (LEO 1530 FESEM, Gemini/Zeiss, Oberkochen, Germany) with EDX capabilities. The standards used were the following natural minerals: Quartz (O), Albite (Na), MAD-10 (K), Nb (Nb), Sb (Sb). Grain size measurements were made using the mean intercept length method from at least six different areas of the SEM image. Silver paint acting as electrodes was applied on both surfaces of the samples for both dielectric and piezoelectric property measurements.

The temperature dependence of the dielectric property of the ceramics was measured from 20 Hz to 1 MHz with an LCR meter (HP 4284A, Agilent Technologies, Inc., Palo Alto, USA) attached to a heating chamber. Room temperature automated resistance measurement was made using a high resistance meter (4339B Agilent Technologies Inc., Palo Alto, USA) connected to a measuring robot. The samples sintered at 1080°C were poled

at room temperature for 10 min with a 20 kV/cm electric field. The planar-mode electromechanical coupling factor (k_p), quality mechanical factor (Q_m) and frequency constant (N_p) were measured by the resonance-antiresonance method with an impedance gain phase analyzer (HP 4192A). Polarization hysteresis measurements were carried out using the standard Sawyer-Tower circuit and a complete dipolar hysteresis measurement was performed in 200 sec.

III. Results and Discussion

The effects of substituting Nb^{5+} with Sb^{5+} and sintering at different temperatures on the relative density values of KNN is shown in Table 1. For pure KNN, sintering at 1080°C gave the highest density value (~ 94 %) which decreased as the sintering temperature was increased. Substitution with Sb^{5+} up to 8 mol % did not show any consistent trend in density but between 10 and 14 mol %, the density value increased as the sintering temperature was increased. This shows that substitution with substantial amount of Sb^{5+} to KNN increases the optimum sintering temperature. This observation is similar to what has been reported in the literature although some MnO_2 were added¹⁹. A possible explanation for the high density value with high Sb^{5+} amount could be due to the formation of secondary phases when more than 10 mol % Sb is added.

Table 1. Density of $(\text{K}_{0.5}\text{Na}_{0.5})(\text{Nb}_{1-x}\text{Sb}_x)\text{O}_3$ sintered at 1080°C, 1090°C and 1100°C respectively. The Lattice parameters, resistance, K_p , Q_m and N_p values were obtained from samples sintered at 1080°C.

mol % Sb	Bulk Density (g/cm^3)			Lattice parameter (\AA)			Resistivity ($\Omega\cdot\text{cm}$)	K_p	Q_m	N_p
	@1080°C	@1090°C	@1100°C	a	b	c	@1080°C	@1080°C	@1080°C	@1080°C
0	4.22 ± 0.04	4.11 ± 0.04	3.99 ± 0.05	3.94744	5.64043	5.6702	1.35E9 ± 7.93E8	0.27	1.73E+01	3152.7
2	4.18 ± 0.07	4.25 ± 0.04	4.23 ± 0.02	3.94986	5.63788	5.6643	9.13E9 ± 1.84E9	0.38	1.24E+01	3218.7
4	4.06 ± 0.03	4.21 ± 0.02	4.19 ± 0.01	3.95444	5.63569	5.6583	2.22E11 ± 1.31E11	0.46	6.20E+00	2253.9
6	4.14 ± 0.06	4.23 ± 0.02	4.24 ± 0.02	3.95432	5.63158	5.6461	1.07E11 ± 3.52E10	0.29	1.65E+01	2983.6
8	4.3 ± 0.07	4.18 ± 0.04	4.19 ± 0.02	3.95774	5.62538	5.6381	3.66E9 ± 2.8E9	0.33	16.4	2717.4
10	4.07 ± 0.05	4.26 ± 0.02	4.57 ± 0.03	3.95901	5.61942	5.6322	8.29E8 ± 1.11E8	0.27	13.4	2634.3
12	4.35 ± 0.05	4.37 ± 0.05	4.53 ± 0.04	3.96627	5.61309	5.6406	3.13E9 ± 9.2E8	0.32	10.3	3061.7
14	4.29 ± 0.15	4.33 ± 0.04	4.56 ± 0.03	3.96248	5.61151	5.6343	2.12E9 ± 1.31E9	0.25	9.68	2275.3

The XRD patterns for $(\text{K}_{0.5}\text{Na}_{0.5})(\text{Nb}_{1-x}\text{Sb}_x)\text{O}_3$ ceramics sintered at 1080°C are as shown in Figure 1a. The pattern for the pure KNN showed minute extra peaks which could not be identified from the database while the patterns between 2 and 10 mol % Sb content have a single orthorhombic phase. Above 10 mol %, extra peaks began to appear and a search and match operation using EVA (commercial software by Bruker) indicated that the extra peaks are related to PDF 01-083-1899 from the International Centre for Diffraction Data (ICDD) database. This phase has a formula $(\text{K}_2\text{NaSb}_3\text{O}_9)$ with a Laue group (cP64) and crystallizes in a cubic structure. It is an ordering variant of KSbO_3 with splitting of one of the cation sites. Lin et al¹⁹ reported that Sb is believed to diffuse into the KNN lattice and form a solid solution with a single perovskite structure but this occurs when

its solid solubility limit is not exceeded. It could also be that the addition of Mn increases the solid solubility limit of Sb^{5+} in KNN thereby suppressing the formation of a second phase.

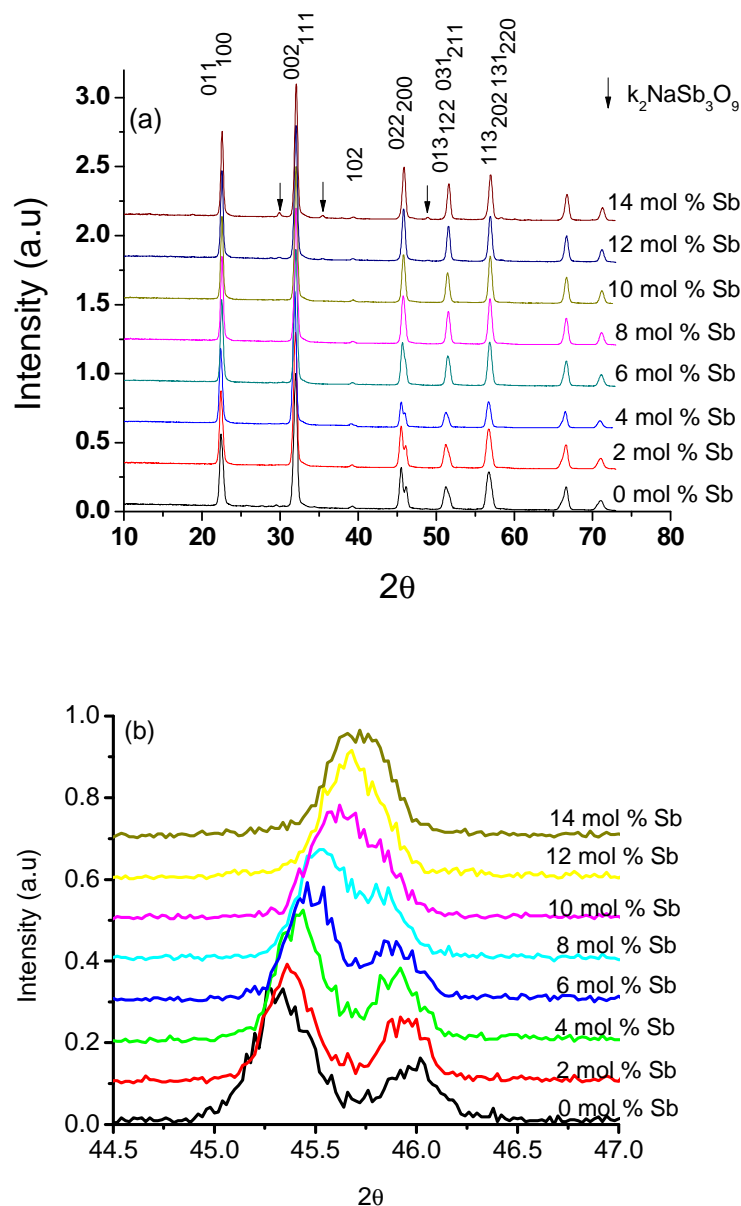


Figure 1. XRD patterns of the polished surfaces of $(\text{K}_{0.5}\text{Na}_{0.5})(\text{Nb}_{1-x}\text{Sb}_x)\text{O}_3$ ceramics sintered at 1080°C for 2 h where x ranges from 0 to 14 mol % Sb (a) showing 2θ values from 10° to 73° and the extra peaks shown with arrows are related to $\text{K}_2\text{NaSb}_3\text{O}_9$ (b) Enlarged pattern from 44.5° to 47° showing the reduction in peak splitting as the amount of antimony substituted is increased.

An enlarged portion of the pattern between 44.5° and 47° is shown in Figure 1b. When the amount of Sb^{5+} substituted is more than 8 mol %, the phase transformed from orthorhombic to pseudo-cubic which is similar to related reports in the literature¹⁹. Based on the difference in ionic radius between Sb^{5+} (0.62 \AA) and Nb^{5+} (0.69 \AA), it was expected that there will be an increase in the distortion of the lattice but this did not occur and rather a structure that is pseudo-cubic with increasing Sb^{5+} content was formed. The excessive lattice vacancies that occur as a result of wide difference in ionic radius lower the solid solution.

KNbO_3 with PDF number 01-071-0946 in the ICDD database was used as a reference because it is isostructural with KNN. The whole powder pattern decomposition was carried out using the Le bail method in Topas. With

increasing amount of Sb^{5+} in KNN, lattice constant a increases while b and c decreases resulting in a decrease of the volume of the unit cell as shown in Table 1.

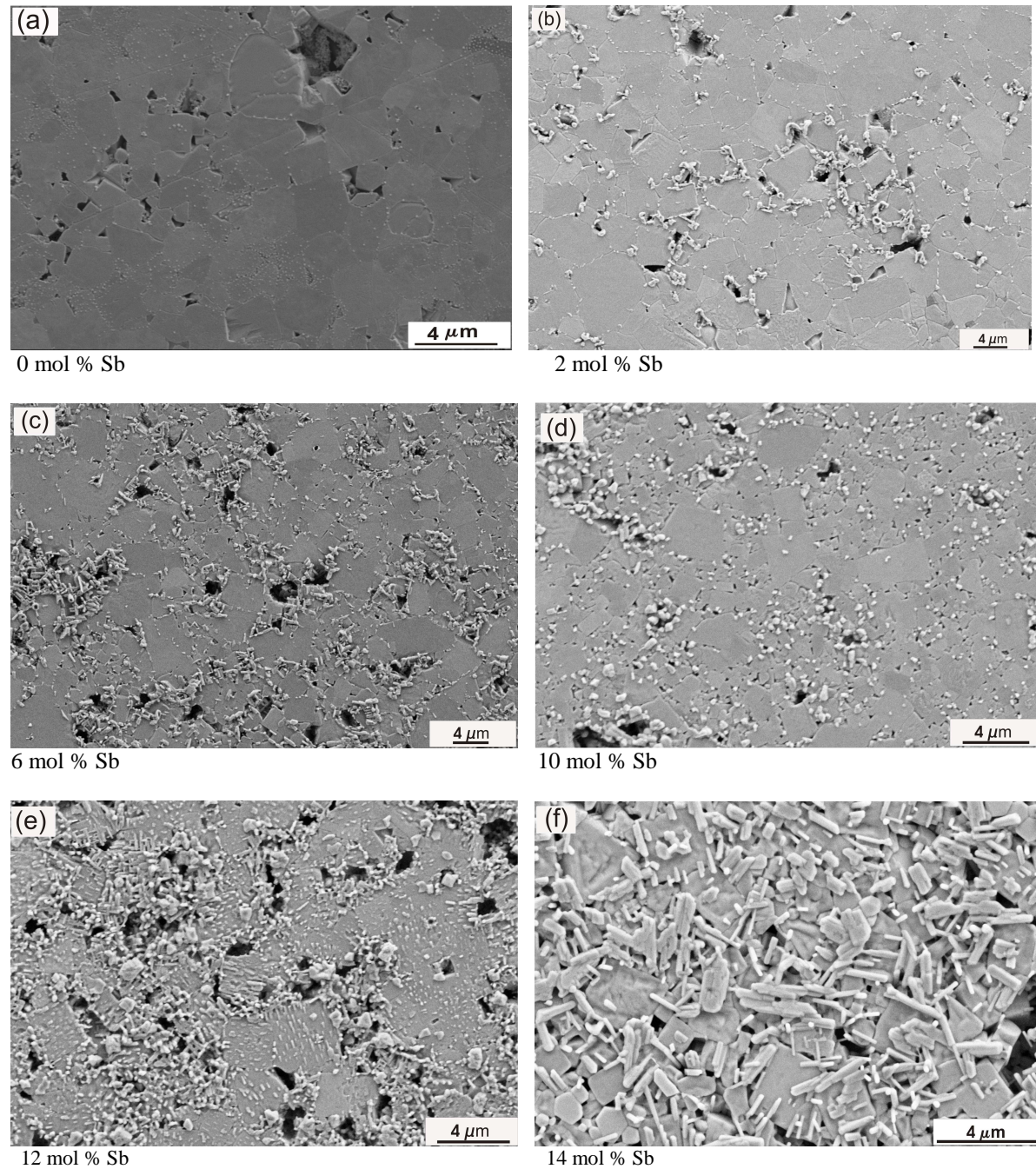


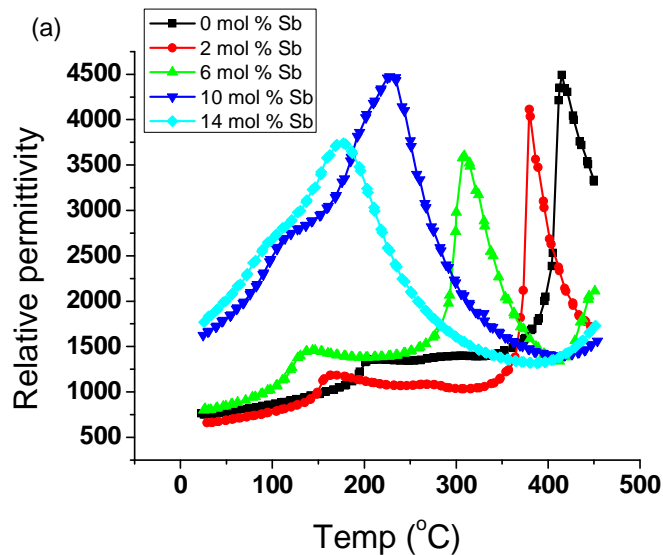
Figure 2. SEM micrographs of KNN ceramics sintered at 1080°C and doped with 0, 2, 6, 10, 12 and 14 mol % Sb (2a, 2b, 2c, 2d, 2e and 2f) respectively. The second phases can be seen clearly on both the grain boundary and inside the grains.

Figure 2a shows the microstructure of a polished and thermally etched pure KNN sample with many small and few big pores located mainly at the triple junction of the grain boundary. The grains have a unimodal size distribution with an average size of $1.51 \pm 0.9 \mu\text{m}$. When 2 mol % of Sb^{5+} was added (Figure 2b), solute precipitation could be observed mainly at the grain boundaries. Chemical etching in oxide ceramics preferentially dissolve certain grains thereby revealing a significant amount of the grain boundary precipitate²⁰. This phenomenon could possibly have occurred for all the samples containing Sb^{5+} and this boundary segregation occurred mainly due to ionic misfit in the perovskite structure. There was increased grain growth with an average size of $2.64 \pm 1.53 \mu\text{m}$. This size distribution shows that some grains were quite large while

others were small. As more Sb^{5+} was substituted for Nb^{5+} , the growth of the new phase also increased forming well ordered clusters which are located mainly at the boundaries (Figure 2c). The size of the grains decreased with increased Sb content with an average size of $2.47 \pm 1.44 \mu\text{m}$. 10 mol % Sb content reduced the grain size to $1.24 \pm 0.59 \mu\text{m}$ (Figure 2d). With 12 mol % Sb^{5+} substitution, (Figure 2e), the growth of the new phase became more pronounced forming an interconnected network both inside the grains and at the boundaries. The average grain size increased to $1.5 \pm 0.58 \mu\text{m}$. With 14 mol % Sb^{5+} (Figure 2f), the new phase grew such that they almost completely covered the grains. This observation is similar to the report by *Li et al* where the Sb^{5+} rich phase showed plate-like shapes²¹. The grain decreased further with an average size of $1.04 \pm 0.76 \mu\text{m}$.

Quantitative element analysis was also carried out on some of the samples by selecting an area of approximately $1 \mu\text{m}$ by $1 \mu\text{m}$ on the surface of the sample. In addition, scans were carried out on the main and precipitate phase for the sample with 14 mol % Sb. The atomic percent of Na, K, Nb, Sb and O were normalized assuming ABO_3 stoichiometry in all cases and a summary of the quantitative element analysis result for the samples is shown in Table 2. The values were obtained after iterating for 5 times and then normalizing them. In the main grains, while Nb^{5+} amounts were more or less within the limits, K^+ and Na^+ amounts were always deficient for all the samples. In most cases, the measured value for Na^+ was on average about 30 % less than the expected value while K^+ was less by about 15 %. Sb^{5+} amount was less in most cases by about 20 % while oxygen amount in all cases was higher than the expected value.

The rod-like grains contain the Sb^{5+} rich phase with close to 3 times more Sb^{5+} than in the normal grains. This shows that Sb^{5+} has a tendency to concentrate mainly at the grain boundaries in KNN. There are a lot of combined reasons for this occurrence but one of the dominant driving forces is the difference in electrostatic potential between the main and the new phase. It occurs due to the presence of aliotropic solutes which tend to segregate in the space charge region²²



The temperature dependence of the relative permittivity values for the samples measured at 100 kHz is as shown in Figure 3a. A relative permittivity value of about 700 was obtained for pure KNN at room temperature which is high compared to what has been previously reported in the literature^{2,3}. A possible explanation could be the slight change in the stoichiometry of the ceramic due to the presence of A-site vacancies in the perovskite. Substitution with very small amount of Sb^{5+} initially decreased the dielectric constant values while the reverse was the case when more dopant was added.

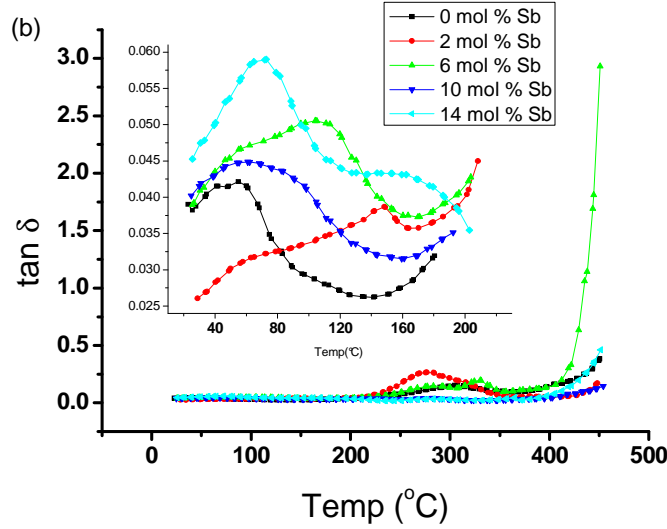


Figure 3 (a) Relative permittivity (ϵ_r) values for $(K_{0.5}Na_{0.5})(Nb_{1-x}Sb_x)O_3$ ceramics measured at 100 kHz as a function of temperature. (b) Dielectric loss ($\tan \delta$) values for the same compositions as a function of temperature measured at 100 kHz. The inset shows an enlarged portion of the diagram from 25°C to 200°C.

Both phase transition points (T_C and T_{T-O}) shifted to lower temperature with increasing Sb^{5+} content. The decrease in the lattice constants with increasing Sb^{5+} substitution accompanies the lowering of the Curie point. The values obtained for both phase transitions for pure KNN ($T_C = 412^\circ\text{C}$, $T_{T-O} = 202^\circ\text{C}$) are similar to what has been reported earlier³. The T_{T-O} could not be observed for the sample with 14 mol % Sb while the sharpness of the peaks at both T_{T-O} and T_C decreased with increasing Sb^{5+} content indicating decreasing ferroelectricity in the sample.

The temperature dependence of the dielectric loss measured at 100 kHz is shown in Figure 3b. At close to room temperature, 2 mol % Sb gives lower loss values (0.026) compared to pure KNN but as Sb^{5+} content is increased, the loss values increases. The inset image inside the figure shows an enlarged region up to 200°C indicating differences in loss values with increasing temperature and different amounts of Sb^{5+} . Above 200°C, the samples with low Sb^{5+} amount have higher loss values when compared with those with higher Sb^{5+} content. Generally the loss values of the samples are moderate considering that there are A-site vacancies in the ceramic.

The resistivity values for the samples measured at room temperature are shown in Table 1. The highest value was obtained for 4 mol% while the lowest was for 10 mol %. Initially Sb substitution increased the resistivity up to $10^{11}\Omega\cdot\text{cm}$ but it decreased when more than 6 mol % was added. This may explain why good polarization could not be obtained for samples with more than 8 mol % Sb.

The polarization-electric field behavior of samples with different molar percentages of Sb is shown in Figure 4. Well saturated hysteresis curves could be obtained for the samples with up to 8 mol % Sb content when a 20 kV/cm field but was not successful with more than 8 mol % Sb due to high leakage current. The remnant polarization (P_r) for pure KNN is $\sim 27 \mu\text{C}/\text{cm}^2$ while the coercive field (E_C) is $\sim 8.8 \text{ kV}/\text{cm}$ and this high value of P_r may probably be due to A-site vacancies in the ceramic. Substitution with Sb decreases the P_r for all the samples but there is no significant change in the E_C ($\sim 9 \text{ kV}/\text{cm}$). The sample with 4 mol % Sb however has the lowest P_r ($9.5 \mu\text{C}/\text{cm}^2$) and E_C ($9.51 \text{ kV}/\text{cm}$).

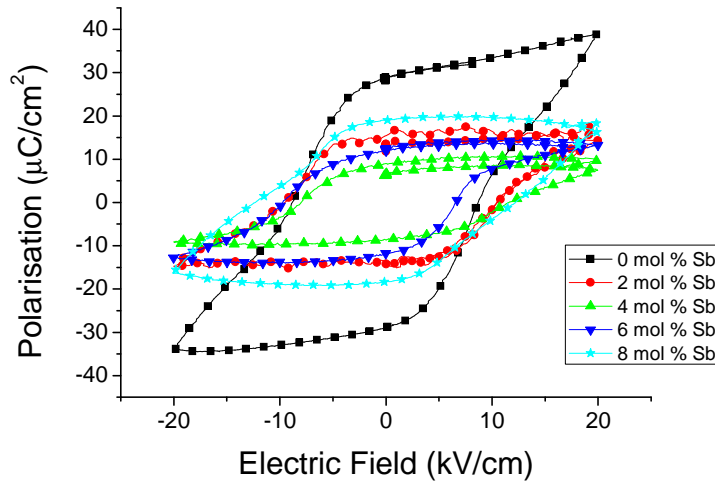


Figure 4. Variation of the polarization field (P - E) hysteresis loops for $(K_{0.5}Na_{0.5})(Nb_{1-x}Sb_x)O_3$ ceramics sintered at 1080°C

The planar-mode electromechanical coupling factor (K_p), quality mechanical factor (Q_m) and frequency constant (N_p) for Sb^{5+} substituted KNN measured at room temperature is given in Table 1. Small Sb^{5+} substitution in KNN increased the K_p from 0.277 for pure KNN to 0.46 for 4 mol % Sb but further substitution decreased the value. The lowest value was obtained for sample the with 14 mol %. The Q_m values for all the samples is low compared to previous reports in the literature¹⁹. The obtained values ranged from 6.2 (4 mol % Sb) to 17.3 for pure KNN which indicates that small Sb substitution initially decreased Q_m but it subsequently increased with more Sb^{5+} . Increase in the density of oxygen vacancies enhances Q_m by pinning the movement of the domain walls but EDX analysis showed that there was A-site vacancy and this may explain why low Q_m values were obtained. The apparent density value of the sample can also affect the obtained Q_m with higher values obtained with denser samples. There was no consistent trend in the obtained N_p values which range from 2254 (4 mol % Sb) to 3219 (2 mol % Sb). All the samples showed high N_p values which indicate high elastic hardness and its suitability for high frequency application.

Table 2. EDX element ratio showing the actual and expected atom % of the different elements in the $(K_{0.5}Na_{0.5})(Nb_{1-x}Sb_x)O_3$ ceramics.

Element	Atomic %	0 mol % Sb	2 mol % Sb	6 mol % Sb	10 mol % Sb	14 mol % Sb (dark)	14 mol % Sb (bright)
O	Actual	65.63	67.22	65.79	65.48	68.38	70.03
	Expected	59.99	59.98	59.99	59.99	59.99	59.99
Na	Actual	6.53	7.19	7.21	6.91	6.58	6.31
	Expected	10.03	10.04	10.04	10.03	10.04	10.04
K	Actual	8.33	7.94	8.36	8.79	7.92	7.86
	Expected	9.99	9.99	9.99	9.99	9.99	9.99
Nb	Actual	19.5	17.44	17.71	17.08	15.07	9.31
	Expected	19.98	19.58	18.78	17.98	17.18	17.18
Sb	Actual		0.2	0.92	1.74	2.05	6.49
	Expected		0.4	1.2	2	2.8	2.8

IV. Conclusion

The effect of substituting niobium with antimony on the crystal structure, piezoelectric and dielectric properties of KNN ceramics produced through the conventional solid state synthesis technique was investigated.

Substituting Nb^{5+} with Sb^{5+} in KNN raises its effective sintering temperature and improves densification.

A phase change in the structure of KNN from orthorhombic to pseudo-cubic was observed above 10 mol % substitution and the microstructures of the ceramic with different amounts of Sb^{5+} show rod-like solute segregation mainly at the grain boundary forming and also inside the grains. This second phase ($\text{K}_2\text{NaSb}_3\text{O}_9$) was rich in Sb^{5+} and EDX analysis showed that there were A-site vacancies in the ceramics. The temperatures of both phase transitions were lowered with increasing Sb^{5+} content such that above 10 mol % Sb, the T_{T-O} decreased to below room temperature. At temperatures below 100°C, substituting more Sb^{5+} led to higher relative permittivity and dielectric values. Saturation polarization was achieved for samples ≤ 8 mol % when a 20 kV/cm field was applied but a good hysteresis loop could not be obtained for those with > 8 mol % due to high leakage current. The sample with 4 mol % Sb substitution gave the highest value of K_p , resistivity and lowest values for Q_m and N_p .

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